

Dividing Polynomials Using Synthetic Division

Divide.

1) $(r^3 + 6r^2 - 21r - 18) \div (r - 3)$

$$\begin{array}{r} 3 | 1 & 6 & -21 & -18 \\ & \downarrow 3 & 27 & 18 \\ \hline 1 & 9 & 6 & 0 \end{array}$$

$$\boxed{r^2 + 9r + 6}$$

3) $(9x^3 - 19x^2 - 28x + 12) \div (x - 3)$

$$\begin{array}{r} 3 | 9 & -19 & -28 & 12 \\ & \downarrow 27 & 24 & -12 \\ \hline 9 & 8 & -4 & 0 \end{array}$$

$$\boxed{9x^2 + 8x - 4}$$

5) $(x^3 + 15x^2 + 45x - 25) \div (x + 5)$

$$\begin{array}{r} -5 | 1 & 15 & 45 & -25 \\ & \downarrow -5 & -50 & 25 \\ \hline 1 & 10 & -5 & 0 \end{array}$$

$$\boxed{x^2 + 10x - 5}$$

2) $(x^3 - 11x^2 + 22x + 40) \div (x - 5)$

$$\begin{array}{r} 5 | 1 & -11 & 22 & 40 \\ & \downarrow 5 & -30 & -40 \\ \hline 1 & -6 & -8 & 0 \end{array}$$

$$\boxed{x^2 - 6x - 8}$$

4) $(m^3 - 13m^2 + 24m + 18) \div (m - 3)$

$$\begin{array}{r} 3 | 1 & -13 & 24 & 18 \\ & \downarrow 3 & -30 & -18 \\ \hline 1 & -10 & -6 & 0 \end{array}$$

$$\boxed{x^2 - 10x - 6}$$

6) $(a^3 + 5a^2 + 14a + 16) \div (a + 2)$

$$\begin{array}{r} -2 | 1 & 5 & 14 & 16 \\ & \downarrow -2 & -6 & -16 \\ \hline 1 & 3 & 8 & 0 \end{array}$$

$$\boxed{x^2 + 3x + 8}$$

$$7) (2x^3 + 9x^2 + 2x - 21) \div (x + 3)$$

$$\begin{array}{r} 2 \longdiv{9 \ 2 \ -21} \\ \downarrow -6 \ 9 \ 21 \\ \hline 2 \ 3 \ \boxed{-10} \end{array}$$

$$2x^2 + 3x - 7$$

$$9) (n^3 + 6n^2 + 4n - 2) \div (n + 1)$$

$$\begin{array}{r} 1 \longdiv{6 \ 4 \ -2} \\ \downarrow -1 \ 5 \ \cancel{+1} \\ \hline 1 \ 5 \ -1 \ \boxed{-6} \end{array}$$

$$x^2 + 5n - 1 - \frac{1}{n+1}$$

$$11) (5x^3 - 2x^2 + 5x - 16) \div (x - 1)$$

$$\begin{array}{r} 1 \longdiv{5 \ -2 \ 5 \ -16} \\ \downarrow 5 \ 3 \ 8 \\ \hline 5 \ 3 \ 8 \ \boxed{-8} \end{array}$$

$$5x^2 + 3x + 8 - \frac{8}{x-1}$$

$$13) (b^3 + 2b^2 - 15b + 49) \div (b + 6)$$

$$\begin{array}{r} -6 \longdiv{1 \ 2 \ -15 \ 49} \\ \downarrow -6 \ 24 \ -54 \\ \hline 1 \ -4 \ 9 \ \boxed{-5} \end{array}$$

$$b^2 - 4b + 9 - \frac{5}{b+6}$$

$$8) (10r^3 - 22r^2 - 17r - 21) \div (r - 3)$$

$$\begin{array}{r} 3 \longdiv{10 \ -22 \ -17 \ -21} \\ \downarrow 30 \ 24 \ 21 \\ \hline 10 \ 8 \ 7 \ \boxed{-10} \end{array}$$

$$10r^2 + 8r + 7$$

$$10) (7m^3 + 16m^2 - 7m + 27) \div (m + 3)$$

$$\begin{array}{r} -3 \longdiv{7 \ 16 \ -7 \ 27} \\ \downarrow -21 \ 15 \ -24 \\ \hline 7 \ -5 \ 8 \ \boxed{13} \end{array}$$

$$7m^2 - 5m + 8 + \frac{3}{m+3}$$

$$12) (r^3 - 5r^2 - 3r + 26) \div (r - 4)$$

$$\begin{array}{r} 4 \longdiv{1 \ -5 \ -3 \ 24} \\ \downarrow 4 \ -4 \ -28 \\ \hline 1 \ -1 \ 7 \ \boxed{-2} \end{array}$$

$$r^2 - r - 7 - \frac{2}{r-4}$$

$$14) (n^3 + 13n^2 + 40n + 26) \div (n + 9)$$

$$\begin{array}{r} -1 \longdiv{1 \ 13 \ 40 \ 26} \\ \downarrow -9 \ -36 \ -36 \\ \hline 1 \ 4 \ 4 \ \boxed{-10} \end{array}$$

$$n^2 + 4n + 4 - \frac{10}{n+9}$$